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60 19 .(0.81) (ANCOVA)  $(0.05=\alpha)$ : 2007 .(40 (NCTM) 2000 (National Council of Teachers of Mathematics)

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(5
                                                                           (Asli, 2001, p. 18)
                                                                (Golden and Shteingold, 2001)
 (Friedlander and Tabach,
                                             2001)
                (Andrew and Catherine, 1996)
                                                             (Coulompe and Berenson, 2001)
                                                          (Lesh, Post and Behr,
                                                                                                  1987, p. 34)
                  .(1994
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(Gloeckner et al., 1995)
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Nasser, 2000)
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(Adiguzel and Akpinar, 2003)
          (Hail, 2000)
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                                                     2003)
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                                            29
                                                                                        .(NCTM, 2000)
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·	( )	969	
·		( ) (stepwise) ( ) paired–sample t-test .independent –sample t-test	
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.(2002
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                                                    (Trends in
                                                    International Mathematics and Science Study (TIMSS),
               (NCTM, 2000)
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(22) Sciences)

(MANCOVA)

(ANCOVA)

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(0.65 -0.3)

(0.7

(0.83).(1987

19

(a)

(1)

30	10.852	3.352	10.93	
30	8.048	2.810	7.97	( )
30	11.930	4.488	12.00	
30	9.336	5.330	9.27	( )

(2)

				(λ)	
0.005	55	2	5.929	0.823	

(3) (ANCOVA)

	( )					
0.315	1.028	9.827	1	9.827	(	)
*0.001	11.0853	113.329	1	113.329		
		9.562	57	545.006		
			59	686.850		

: (1)

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 $(0.05=\alpha)$  .(2.594)

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(4) (ANCOVA)

	( )						
0.093	2.923	68.671	1	68.671	(	)	
*0.043	4.277	100.486	1	100.486			
		23.495	57	1339.196			
			59	1519.933			

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## The Effect of Using Multiple Mathematical Representations on the Attainment of Mathematical Concepts Among Basic Eighth Grade Students and their Ability to Solve Verbal Problems

Riyad Ibrahim Al-Balasi and Areej Isam Barham\*

## **ABSTRACT**

This study aims at investigating the effect of using multiple mathematical representations on the attainment of mathematical concepts and the ability to solve verbal problems by the eighth grade students in the Functions and Relations unit. The study sample consisted of 60 students from Al-Hamra Secondary School for boys in the education district of Northern Badia at the Governorate of Al- Mafraq. The participators were randomly divided into two groups: the experimental group was taught by using the multiple mathematical representations method and the control group was taught by the traditional method. To achieve the goals of the study, two tests were built. The first was to measure the acquisition extent of mathematical concepts by students. It consisted of (19) "multiple choice" items. The second test was to measure students' ability in solving verbal problems. The test consisted of (4) "essay" items. The validity of the tests was established by a group of specialized judges in mathematics, measurement and evaluation. The two tests were performed on an exploratory sample outside the study sample to achieve reliability and analysis of the two tests. Acquisition of concepts was established using Pearson correlation method. Results revealed that there were statistically significant difference ( $\alpha = 0.05$ ) between study sample subjects on the attainment of mathematical concepts and the ability to solve verbal problems, attributed to the method of instruction, in favor of the experimental group.

Keywords: Multiple Mathematical Representations, Mathematical Concepts, Solving Verbal Problems.

<sup>\*</sup> Ministry of Education; and Faculty of Education, The Hashemite University, Jordan. Received on 20/2/2008 and Accepted for Publication on 31/7/2008.